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The Queue Abstract Type

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Queue

- A *queue* is an *ordered list* in which *insertions* (or called *additions* or *pushes*) and *deletions* (or called *removals* or *pops*) are made at *different ends*.
- New elements are inserted at *rear* end.
- Old elements are deleted at *front* end.

insertion | rear | front | deletion

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Queue Operations

- Insert a new element into queue
  - f: front position
  - r: rear position

| Insert A | Insert B | Insert C |

-1 | A | B A | C B A

r f | r f | r f | r   f

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Queue Operations

- Delete an old element from queue
  - ◦ f: front position
  - ◦ r: rear position

| C | B | A |
r   f

Delete →

| C | B |
r   f

Delete →

| C |
r f

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Problems

- What happen if rear == capacity-1 ?

| J | I | H | G | ... |
r   f

- Add more space ? wasted

| | | | | J | I | H | G | ... |
r   f

- Shift right?   Codes are complicated…

| . | . | . | J | I | H | G |
r   f

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Circular Queue

rear   rear   rear

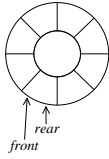Initial   Insertion   Deletion

`front = (front+1) % capacity;`
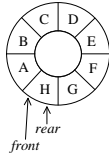
`rear = (rear+1) % capacity;`

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When is the Queue Empty?

- rear == front ? NO!

Queue is empty

Queue is full

Allocate extra space before the queue is full

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Queue: ADT

```
template < class T >
class Queue // A finite ordered list
{
public:
        // Constructor
        Queue (int queueCapacity = 10);

        // Check if the stack is empty
        bool IsEmpty ( ) const;

        // Return the front element
        T& Front ( ) const;

        // Return the rear element
        T& Rear ( ) const;

        // Insert a new element at rear
        void Push (const T& item);

        // Delete one element from front
        void Pop ( );
private:
        T* queue;
        int front, rear; // init. value = -1
        int capacity;
};
```

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Queue Operations

```
template < class T >
void Queue < T >::IsEmpty() const { return front==rear; }

template < class T >
T& Queue < T >::Front() const {
   if(IsEmpty()) throw "Queue is empty!";
   return queue[(front+1)%capacity];
}

template < class T >
T& Queue < T >::Rear() const {
   if(IsEmpty()) throw "Queue is empty!";
   return queue[rear];
}
```

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Queue Operations: Push & Pop

```
template < class T >
void Queue< T >::Push (const T& x)
{    // Add x at rear of queue
    if((rear+1)%capacity == front)
    {
        // queue is going to full, double the capacity!
    }
    rear = (rear+1)%capacity;
    queue [rear] = x;
}
```
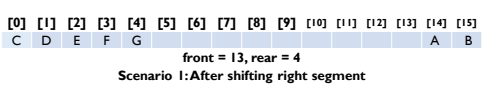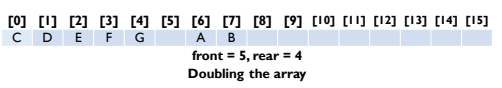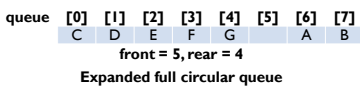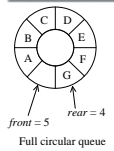
```
template < class T >
void Queue < T >::Pop ( )
{    // Delete front element from queue
    if(IsEmpty()) throw "Queue is empty. Cannot delete.";
    front = (front+1)%capacity;
    queue[front].~T(); // Delete the element
}
```
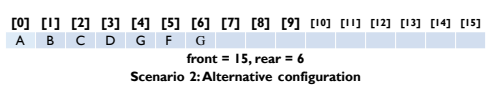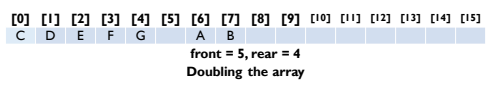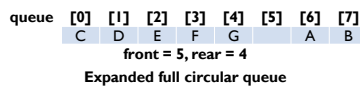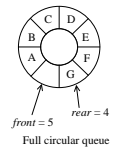
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Doubling Queue Capacity

queue	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]
	C	D	E	F	G		A	B

front = 5, rear = 4
Expanded full circular queue

front = 5
Full circular queue

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	[15]
C	D	E	F	G		A	B								

front = 5, rear = 4
Doubling the array

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	[15]
C	D	E	F	G										A	B

front = 13, rear = 4
Scenario 1: After shifting right segment

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Doubling Queue Capacity

queue	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]
	C	D	E	F	G		A	B

front = 5, rear = 4
Expanded full circular queue

front = 5
Full circular queue

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	[15]
C	D	E	F	G		A	B								

front = 5, rear = 4
Doubling the array

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	[15]
A	B	C	D	G	F	G									

front = 15, rear = 6
Scenario 2: Alternative configuration

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